TOPOLOGICAL CHARACTERIZATION OF TRIVIAL COHOMOLOGY WITH SOME APPLICATIONS.

ANDRZEJ CZARNECKI

ABSTRACT. We present a simple theorem sitting between topology and homotopy theory: trivial first cohomology of a compact manifold is equivalent to some cutting properties of open sets. This can be regarded as some kind of local-to-global principle, and gives apparently new insight into topology of Euclidean spaces. We can generalize this to finite and finite type CW-complexes. Some applications to complex analysis and differential equations are also explained.

Faculty of Mathematics and Computer Sciences, Jagiellonian University $E\text{-}mail\ address:\ \texttt{andress:}\ \texttt{a$

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